

Example from Braatz, Chapter 1, Example 3

Fiel: Ch02_Braatz.m

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Problem Statement

Consider a liquid surge vessel with a steady-state volume of 500 liters and steady-state inlet and outlet flow rates of 50 liters/minute. Determine the liquid volume as a function of time if the inlet flow rate is $F_{in}(t) = 50 + 10 \sin(0.1t)$ and the outlet flow rate remains constant at 50 (both flow rates are in units of liters/minute). The liquid is a dilute aqueous solution.

Problem Parameters

The problem does not specify an initial condition, or a time span for simulation which are added here.

```
tspan = [0 600];  
Vinitial = 100;  
Vmin = 0;  
Vmax = 500;
```

Inputs and Outputs

The inputs and outputs are expressed as functions of time.

```
Fin = @(t) 50 + 10*sin(0.1*t);  
Fout = @(t) 50;
```

Create the ODE Model

A model consisting of a differential equation is expressed as a function of the independent variable time, and of the state variable Volume.

```
f = @(t,V) Fin(t) - Fout(t);
```

Integration

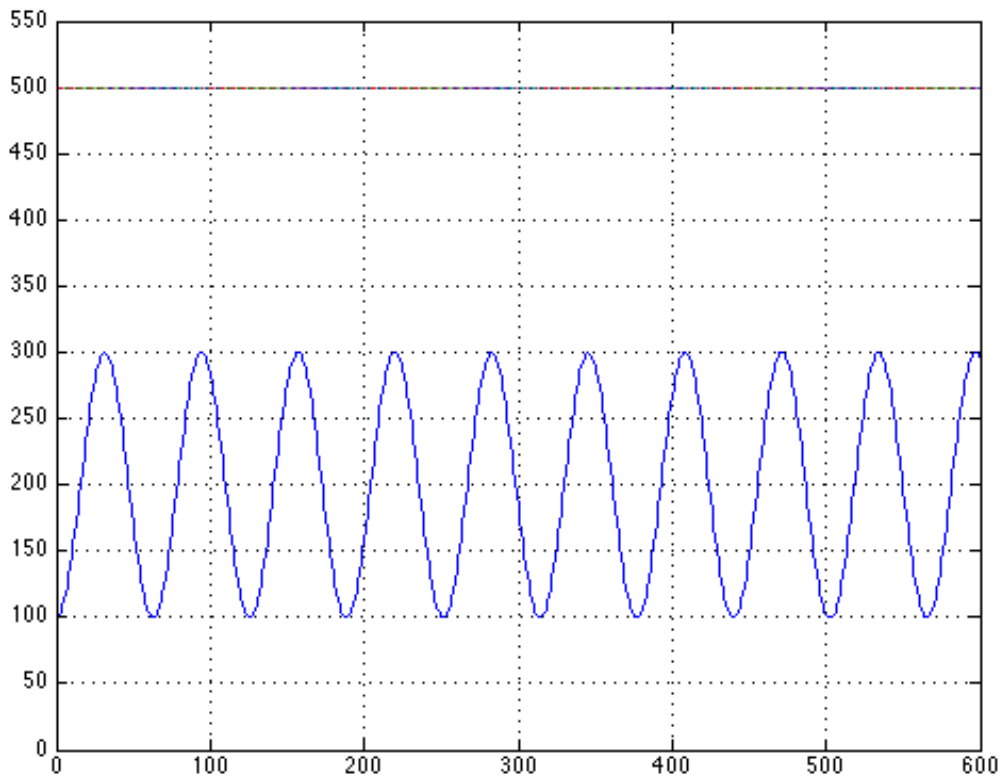
```
Vsoln = ode45(f, tspan, Vinitial);
```

Evaluate the Solution

```
t = min(tspan):max(tspan);  
V = deval(Vsoln,t);
```

Plot

```
plot(t,V,t,Vmin,t,Vmax,'Linewidth',1.5);  
axis([min(tspan) max(tspan) 0.9*Vmin 1.1*500]);  
grid;
```



Annotate the plot

The following annotations are a minimal set that should be part of every plot.

```
title('Liquid Surge Vessel');  
xlabel('Time [minutes]');  
ylabel('Volume [liters]');  
legend('Volume', 'Lower Limit', 'Upper Limit');
```

